



## Supervised Learning

- Neural Nets
- Feedforward
- BackProp
- Success

## Decision Trees

# Supervised Learning

# Neural Nets

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- regression: given inputs and outputs, find good weights of input nodes
- neural networks: given inputs and outputs, introduce hidden layers and find good weights
- start with random weights and adjust based on perceived error

Activation function: the output of each node is based on the weighted sum of inputs, run through a nonlinear function (often sigmoid)

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

Nonlinear activation function means nonlinear system behavior

# Neural Nets

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# Feedforward

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- With good weights, a neural net has a good approximation function: inputs and outputs match the training data
- Feed the input, calculate the values of each node, check the outputs
- Initial weights were random, though!
- We need to change weights for every connection to decrease the output error

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# Back-propagation

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- After feeding input values forward, we have a prediction for the output
- Based on this prediction and the actual labeled output, we trace error backwards through system

For the last set of weights:

$$\begin{aligned}W_{i,j} &= W_{i,j} - \alpha \left( \frac{\delta Error}{\delta W_{i,j}} \right) \\ &= W_{i,j} - \alpha \Delta_i\end{aligned}$$

To update hidden layer weights, we use weighted sum of changes

$$W_{i,j} = W_{i,j} + \alpha \sum_j W_{i,j} \Delta_j$$



# Successful Neural Nets

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- +: Neural nets perform better with multiple hidden layers
- +: Excellent results for many training sets
- -: Training is computationally intensive
- -: Weights and hidden nodes are not intuitive

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# Decision Trees

# Example

Example	Input Attributes										Output
	<i>Alt</i>	<i>Bar</i>	<i>Fri</i>	<i>Hun</i>	<i>Pat</i>	<i>Price</i>	<i>Rain</i>	<i>Res</i>	<i>Type</i>	<i>Est</i>	
$x_1$	<i>Yes</i>	<i>No</i>	<i>No</i>	<i>Yes</i>	<i>Some</i>	<i>\$\$\$</i>	<i>No</i>	<i>Yes</i>	<i>French</i>	<i>0-10</i>	$y_1 = \text{Yes}$
$x_2$	<i>Yes</i>	<i>No</i>	<i>No</i>	<i>Yes</i>	<i>Full</i>	<i>\$</i>	<i>No</i>	<i>No</i>	<i>Thai</i>	<i>30-60</i>	$y_2 = \text{No}$
$x_3$	<i>No</i>	<i>Yes</i>	<i>No</i>	<i>No</i>	<i>Some</i>	<i>\$</i>	<i>No</i>	<i>No</i>	<i>Burger</i>	<i>0-10</i>	$y_3 = \text{Yes}$
$x_4$	<i>Yes</i>	<i>No</i>	<i>Yes</i>	<i>Yes</i>	<i>Full</i>	<i>\$</i>	<i>Yes</i>	<i>No</i>	<i>Thai</i>	<i>10-30</i>	$y_4 = \text{Yes}$
$x_5$	<i>Yes</i>	<i>No</i>	<i>Yes</i>	<i>No</i>	<i>Full</i>	<i>\$\$\$</i>	<i>No</i>	<i>Yes</i>	<i>French</i>	<i>&gt;60</i>	$y_5 = \text{No}$
$x_6$	<i>No</i>	<i>Yes</i>	<i>No</i>	<i>Yes</i>	<i>Some</i>	<i>\$\$</i>	<i>Yes</i>	<i>Yes</i>	<i>Italian</i>	<i>0-10</i>	$y_6 = \text{Yes}$
$x_7$	<i>No</i>	<i>Yes</i>	<i>No</i>	<i>No</i>	<i>None</i>	<i>\$</i>	<i>Yes</i>	<i>No</i>	<i>Burger</i>	<i>0-10</i>	$y_7 = \text{No}$
$x_8$	<i>No</i>	<i>No</i>	<i>No</i>	<i>Yes</i>	<i>Some</i>	<i>\$\$</i>	<i>Yes</i>	<i>Yes</i>	<i>Thai</i>	<i>0-10</i>	$y_8 = \text{Yes}$
$x_9$	<i>No</i>	<i>Yes</i>	<i>Yes</i>	<i>No</i>	<i>Full</i>	<i>\$</i>	<i>Yes</i>	<i>No</i>	<i>Burger</i>	<i>&gt;60</i>	$y_9 = \text{No}$
$x_{10}$	<i>Yes</i>	<i>Yes</i>	<i>Yes</i>	<i>Yes</i>	<i>Full</i>	<i>\$\$\$</i>	<i>No</i>	<i>Yes</i>	<i>Italian</i>	<i>10-30</i>	$y_{10} = \text{No}$
$x_{11}$	<i>No</i>	<i>No</i>	<i>No</i>	<i>No</i>	<i>None</i>	<i>\$</i>	<i>No</i>	<i>No</i>	<i>Thai</i>	<i>0-10</i>	$y_{11} = \text{No}$
$x_{12}$	<i>Yes</i>	<i>Yes</i>	<i>Yes</i>	<i>Yes</i>	<i>Full</i>	<i>\$</i>	<i>No</i>	<i>No</i>	<i>Burger</i>	<i>30-60</i>	$y_{12} = \text{Yes}$

Restaurant domain



# Learning a Decision Tree

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Goals:

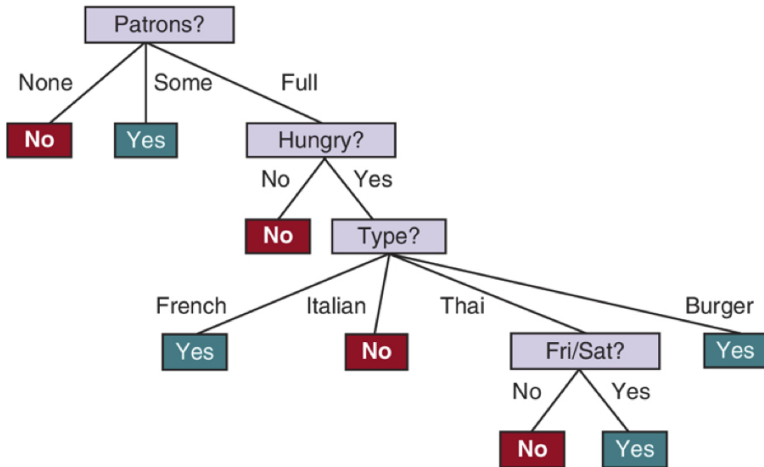
- Decision tree matches data
- Decision tree is small (fewer nodes, smaller height)

Approach:

- Analyze attributes for best simplification
- Split examples based on that attribute
- For all values of attribute, find remaining best attribute...
- Resulting tree is a small tree that makes good predictions

Resulting tree may not match original (unobservable) tree

# Example



Restaurant Decision Tree